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**Heterogeneity in Sectoral Price  
Stickiness, Aggregate Dynamics and  
Monetary Policy Pitfalls with Real  
Shocks<sup>1</sup>**

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1 Heterogeneity in Sectoral Price Stickiness,  
2 Aggregate Dynamics and Monetary Policy Pitfalls  
3 with Real Shocks

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6 **Abstract**

7 Ample differences in sectoral price stickiness is a widely documented fact.  
8 This paper shows that in presence of *real* shocks, heterogeneity in sectoral price  
9 stickiness plays a key role in the determination of the aggregate dynamics. The  
10 larger price stickiness heterogeneity, the smaller the *persistence* of inflation and  
11 the *volatility* of inflation, interest rate and output-gap. Thus, two economies  
12 with the same average degree of sectoral price stickiness but unlike variance  
13 may behave very differently. In terms of monetary policy, they can require *in-*  
14 *terest rate paths* that substantially differ both qualitatively and quantitatively.  
15 Generally, with real shocks, disregarding the dispersion in sectoral price stick-  
16 iness leads policymakers to overvalue the variation and persistence of inflation  
17 and output gap.

18 JEL Classification: E31, E32, E37, E52.

19 Key Words: Price Stickiness Heterogeneity, Real Shocks, New Keynesian  
20 model, Persistence, Volatility, Monetary Policy Mistakes.

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# 1 Introduction

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This paper relates heterogeneity in sectoral price stickiness to aggregate macroeconomic dynamics and monetary policy mistakes in presence of real shocks. Real-world economies feature multiple sectors differing in terms of nominal rigidities (Altissimo et al. 2006, Blinder et al. 1998, Bils and Klenov, 2004, Dhyne et al. 2006, Nakamura and Steinsson 2008). Most of the research that embeds nominal rigidities, however, adopts a one-sector set up. This is not an innocuous assumption. Indeed, it has been shown both theoretically and empirically that the relation between heterogeneity in sectoral nominal rigidities and macroeconomic dynamics matters in a significant way with monetary shocks. Pioneering this relation, Carvalho (2006) found that the presence of sectoral differences in price stickiness in a New-Keynesian model leads to larger and more persistent real effects in response to monetary shocks. With sticky wage contracts in a Generalized Taylor Economy, Dixon and Kara (2010a) show that for economies with the same average contract length, monetary shocks are more persistent in presence of longer contracts. Empirically, Imbs et al. (2011) show that a Phillips curve based on sectoral estimates implies policy trade-offs remarkably different from one based on aggregate estimates. Focusing on inflation persistence instead of persistence in real variables, Sheedy (2007) finds that heterogeneity in price stickiness leads to less inflation persistence. On the other hand, Dixon and Kara (2010b) argue that considering the distribution of contract length substantially improves the ability of the model to replicate the inflation persistence found in the data.

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This previous literature has related heterogeneity in sectoral nominal rigidities to the persistence of real effects caused by *monetary shock*, and to the model performance at reproducing the inflation persistence in the data. The current paper contributes to this literature by showing that in presence of *real shocks*, neglecting heterogeneity in sectoral price stickiness leads to a wrong assessment of the aggregate dynamics, and consequently, to important monetary policy mistakes.

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The analysis shows that with real shocks, accounting for the dispersion in sectoral price stickiness, the *persistence* of aggregate inflation turns out to be smaller. The same result occurs with the *variability* of aggregate inflation, interest rate and output-gap. The investigation suggests that these findings are quantitatively important too. Interestingly, this implies that two economies sharing the mean degree of price stickiness but not the variance may respond to real disturbances very differently and thus deserve specific monetary policies. In particular, they can require paths for

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55 expected interest rates that remarkably differ both qualitatively and quantitatively.  
56 Generally, when real disturbances hit the economy, disregarding the dispersion in  
57 sectoral price stickiness leads policymakers to overvalue the variation and persistence  
58 of inflation and the variation of the output gap and the interest rate.

59 We believe that these implications pose serious problems to monetary policy de-  
60 cisions. In particular, the use of one-sector model would corrupt the projections  
61 of the target variables which are fundamental ingredients for the inflation target-  
62 ing operating procedure in use at several central banks (Svensson 2010). Thus, this  
63 work questions the prominent use of one-sector models for economic estimations and  
64 forecasts, a view shared with Imbs et al. (2011).

65 The intuition for the current findings is the following. Heterogeneity in sectoral  
66 price stickiness introduces the relative price of sectoral goods into the picture. This  
67 variable, affecting sectoral inflations in opposite ways via the demand channel, acts  
68 as a buffering device attenuating the impact of aggregate real shocks on aggregate  
69 inflation. As a consequence, the whole transmission mechanism of the shock to the  
70 economy dramatically changes. Using a graphical AS-AD framework that exactly  
71 embeds expectations reveals that the role played by the relative price consists of  
72 contracting the shifts of the AS due to real shocks. As a result, aggregate inflation  
73 varies less affecting the rest of the economic dynamics.

74 Sectoral and regional heterogeneity in nominal rigidities have been also related by  
75 the previous literature to optimal monetary policy obtaining important results. Aoky  
76 (2001) and Benigno (2004), respectively in two-sector and two-region economies, show  
77 that focusing the policy response on the sector/region with sticky or stickier price  
78 maximizes welfare. A different result is obtained by Kara (2010) with a multiple-  
79 sector Generalized Taylor Economy where targeting economy-wide inflation results  
80 in almost the same welfare of the optimal monetary policy. With respect to this  
81 literature, the current paper is different in that abstracts from optimal monetary  
82 policy. What it does is a) focusing on the impact of heterogeneity in sectoral price  
83 stickiness on the macroeconomic dynamics driven by real shocks, and b) investigating  
84 how the path of the expected interest rate changes neglecting heterogeneity in price  
85 stickiness. This is carried out contrasting a *two-sector economy* featuring sectoral  
86 asymmetry with a *one-sector economy* featuring a degree of price stickiness equal to  
87 the average of the sectoral price stickiness in the two-sector economy.

88 The plan of the paper is as follows. Section 2 presents the model where con-  
89 sumption habits are introduced into an otherwise standard two-sector New-Keynesian

model drawn on Benigno (2004) and Woodford (2011). It derives the non-linear optimal conditions, the log-linearized relations used in the following analysis, and reports the calibration of the structural parameters. Section 3 investigates the relation between sectoral heterogeneity in price stickiness and the dynamics of the economy in presence of cost-push, technology, and preferences shocks. First the main result is illustrated via impulse response functions. Next, the implications in terms of monetary policy mistakes are discussed. Then, the mechanics is explained. Here, the heterogeneity assumption is related to switches in sectoral demands and to their buffering role on aggregate inflation. After that, it is presented a complementary illustration using an appropriate AD-AS graphical framework for the New-Keynesian model. Finally, the analysis is completed looking at autocorrelations, and standard deviations of the endogenous variables. Although this paper focuses on real shocks, Section 4 also offers a parallel with Carvalho (2006) that considers monetary shocks. This comparison shows that introducing the heterogeneity assumption leads to opposite results with monetary and real shocks which, however, always obtain via a contraction in the shift of the AS following the shock. Section 4 also presents three general monetary policy pitfalls in terms wrong assessment of the persistence and volatility in inflation and real activity when policymakers disregard dispersion in sectoral price stickiness. Concluding remarks are in section 5.

## 2 The model

The economy is populated by a continuum of unit mass of identical infinite-lived households each seeking to maximize

$$U_t = E_t \sum_{T=t}^{\infty} \beta^{T-t} \left\{ \tilde{u}(C_T - \eta C_{T-1}; \bar{C}_T) - \int_0^1 \tilde{v}[H_T(j)] dj \right\},$$

where  $\beta$  is the intertemporal discount factor,  $C_t$  represents all interest-rate-sensitive expenditure including investments and is defined as a CES aggregate

$$C_t \equiv \left[ (n_s)^{1/\rho} (C_t^s)^{(\rho-1)/\rho} + (n_m)^{1/\rho} (C_t^m)^{(\rho-1)/\rho} \right]^{\rho/(\rho-1)}, \quad (1)$$

of the goods  $C_t^s$  and  $C_t^m$  which are produced, respectively, by the s and m-sector, with  $\rho$  defining their elasticity of substitution and  $n_s$  and  $n_m$  ( $n_s \equiv 1 - n_m$ ) denoting the number of goods of sector s and m in  $C_t$ , respectively. Each sectoral good is, in

117 turn, a Dixit-Stiglitz aggregate of the continuum of differentiated goods produced in  
118 the sector

$$C_t^h \equiv \left[ n_h^{-\frac{1}{\theta}} \int_{N_h} (C_t^h(i))^{1-\frac{1}{\theta}} di \right]^{\frac{\theta}{\theta-1}}, \quad h = s, m$$

119 where  $\theta > 1$  is the sectoral elasticity of substitution between any two differentiated  
120 goods and  $N_s \equiv [0, n_s]$ ,  $N_m \equiv (n_s, 1]$ . Period preferences on consumption and labour  
121 are modeled as CRRA functions

$$\tilde{u}(C_t - \eta C_{t-1}; \bar{C}_t) = \bar{C}_t^{\frac{1}{\tilde{\sigma}}} \frac{(C_t - \eta C_{t-1})^{1-\frac{1}{\tilde{\sigma}}} - 1}{1 - \frac{1}{\tilde{\sigma}}}, \quad (2)$$

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$$\tilde{v}[H_t(j)] \equiv \frac{H_t^{1+\nu}(j)}{1+\nu}, \quad (3)$$

123 where  $\bar{C}_t$  is an exogenous preference shock,  $H_t(j)$  is the quantity supplied of labour  
124 of type  $j$ ,  $\tilde{\sigma} > 0$  captures the intertemporal elasticity of substitution in consumption,  
125  $0 \leq \eta < 1$  measures the degree of habit persistence, and  $\nu > 0$  is the inverse of the  
126 elasticity of goods production<sup>1</sup>.

127 The price index for the minimum cost of a unit of  $C_t$  is given by

$$P_t \equiv [n_s (P_t^s)^{1-\rho} + (n_m) (P_t^m)^{1-\rho}]^{1/(1-\rho)}, \quad (4)$$

128 with  $P^s$ ,  $P^m$  denoting, respectively, the Dixit-Stiglitz price index for goods produced  
129 in the s and m sector.

130 Preferences captured by equation (1) imply that the optimal sectoral consumption  
131 levels are given by

$$C_t^h = n_h C_t \left( \frac{P_t^h}{P_t} \right)^{-\rho}, \quad h = s, m. \quad (5)$$

132 Financial markets are assumed to be complete so that at any date all households face  
133 the same budget constraint and consume the same amount. Then, utility maximiza-  
134 tion subject to the budget constraint and the no-Ponzi scheme requirement yields the  
135 condition for optimal consumption

$$\lambda_t = \beta E_t \left\{ \frac{[\tilde{u}_c(C_{t+1} - \eta C_t; \bar{C}_{t+1}) - \beta \eta E_t \tilde{u}_c(C_{t+2} - \eta C_{t+1}; \bar{C}_{t+2})] P_t}{\tilde{u}_c(C_t - \eta C_{t-1}; \bar{C}_t) - \beta \eta E_t \tilde{u}_c(C_{t+1} - \eta C_t; \bar{C}_{t+1})} \frac{P_t}{P_{t+1}} \right\}, \quad (6)$$

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<sup>1</sup>It is worth noting that the assumption of habit persistence is not necessary to obtain the results shown below. Nevertheless, this real rigidity captures the gradual hump-shaped response of real spending to various shocks and thus is well accepted in the New-Kenesian literature.

where  $\lambda_t \equiv \frac{1}{1+i_t}$  is the price of a one-period nominal bond. Finally, utility maximization requires that the optimal supply of labour of type  $j$  is given by

$$\Omega_t(j) = \Psi_t \frac{\tilde{v}_h[H_t(j)]}{[\tilde{u}_c(C_t - \eta C_{t-1}; \bar{C}_t) - \eta\beta E_t \tilde{u}_c(C_{t+1} - \eta C_t; \bar{C}_{t+1})]}, \quad (7)$$

where  $\Omega_t(j)$  is the real wage demanded for labour of type  $j$  and  $\Psi_t \geq 1$  is an exogenous markup factor in the labor market assuming that firms are wage-takers.

Moving to production, each household  $i$  is assumed to supply all type of labour and is a monopolistically competitive producer of one differentiated good, either  $y^m(i)$  or  $y^s(i)$ . In this economy any firm  $i$  belongs to an industry  $j$  which, in turn, belongs either to sector  $s$  or  $m$ . Furthermore, there is a unit interval continuum of industries indexed by  $j$  and in each industry there is a unit interval continuum of good indexed by  $i$  so that the total number of goods is one. Since in equilibrium all the firms belonging to an industry will supply the same amount, they will also demand the same amount of labour. As a result the total demand of labour in an industry is equal to demand of labor of any differentiated firm in the industry. Next, we assume industry-specific labor as the only variable input

$$y_t^h(i) = A_t [H_t^h(i)]^{\frac{1}{\phi}}, \quad h = s, m,$$

where  $A_t$  is a technology shock,  $H_t^h(i)$ , is the quantity of labour used by the representative firm  $i$  in the  $h$ -sector to produce good  $i$ , and  $\phi > 1$ , is the elasticity of sectoral output with respect to hours worked.

In equilibrium, market clearing in the goods market requires

$$Y_t^m = C_t^m, \quad Y_t^s = C_t^s, \quad Y_t = C_t. \quad (8)$$

Hence, combining (2), (6), and (8) we obtain the nonlinear version of the New-Keynesian IS relation. Turning to the producers' pricing behaviour, firms in both sectors fix their prices at random intervals following the Calvo (1983) staggered price model and have the opportunity to change their prices with probability  $(1 - \alpha)$ . Thus, a producer  $i$  in the  $h = m, s$  sector that is allowed to set its price in period  $t$  chooses its new price for the random period starting in  $t$ ,  $\tilde{p}_t^h$ , to maximize the flow of expected profits:

$$\max_{\tilde{p}_t^h} E_t \sum_{T=t}^{\infty} \alpha^{T-t} \lambda_{t,T} \left\{ \tilde{p}_t^h y_T^h(i) - \left[ \frac{y_T^h(i)}{A_T} \right]^\phi \Psi_T^h \frac{[y_T^h(j)/A_T]^{\nu\phi} P_T}{\bar{C}_t^{\frac{1}{\sigma}} (C_t - \eta C_{t-1})^{-\frac{1}{\sigma}} - \eta\beta \bar{C}_{t+1}^{\frac{1}{\sigma}} (C_{t+1} - \eta C_t)^{-\frac{1}{\sigma}}} \right\},$$

161 where  $\lambda_{t,T}$  is the stochastic discount factor by which financial markets discount ran-  
 162 dom nominal income in period  $T$ . Accounting for firm  $i$  demand function in sector  
 163  $h$ , and considering that the firm's pricing decision cannot change the real wage, the  
 164 f.o.c. is

$$\begin{aligned}
 0 = E_t \sum_{T=t}^{\infty} \alpha^{T-t} \lambda_{t,T} & \left\{ C_T \left( \frac{\tilde{p}_t^h}{P_T^h} \right)^{-\theta} \left( \frac{P_T^h}{P_T} \right)^{-\rho} - \theta C_T \left( \frac{\tilde{p}_t^h}{P_T^h} \right)^{-\theta-1} \frac{\tilde{p}_t^h}{P_T^h} \left( \frac{P_T^h}{P_T} \right)^{-\rho} - \right. \\
 & \left. \left[ -\phi \theta \left( \frac{C_T}{A_T} \right)^\phi \left( \frac{\tilde{p}_t^h}{P_T^h} \right)^{-\phi\theta-1} \frac{1}{P_T^h} \left( \frac{P_T^h}{P_T} \right)^{-\phi\rho} \right] \frac{\Psi_T^h \left[ C_t \left( \frac{p_t^h(j)}{P_t^h} \right)^{-\theta} \left( \frac{P_t^h}{P_t} \right)^{-\rho} \frac{1}{A_T} \right]^{\nu\phi} P_T}{\bar{C}_T^{\frac{1}{\sigma}} (C_T - \eta C_{T-1})^{-\frac{1}{\sigma}} - \eta \beta \bar{C}_{T+1}^{\frac{1}{\sigma}} (C_{T+1} - \eta C_T)^{-\frac{1}{\sigma}}} \right\}
 \end{aligned} \tag{9}$$

## 166 2.1 Log-linearized relations

167 We now log-linearize the equilibrium conditions around the steady state where the  
 168 variables  $\left( Y_t^m, Y_t^s, Y_t, Q_t, \frac{P_{t+1}}{P_t}, \frac{P_{t+1}^s}{P_t^s}, \frac{P_{t+1}^m}{P_t^m} \right)$  are equal to  $(Y^m, Y^s, Y, 1, 1, 1, 1)$  and all the  
 169 shocks are equal to one. Loglinearizing the Euler equation, account being taken of  
 170 the market clearing condition, leads to the IS relation

$$\begin{aligned}
 y_t = \frac{\eta}{1 + \eta(1 + \beta\eta)} y_{t-1} + \frac{1 + \eta\beta(1 + \eta)}{1 + \eta(1 + \beta\eta)} y_{t+1|t} - \frac{\eta\beta}{1 + \eta(1 + \beta\eta)} y_{t+2|t} \\
 - \frac{\tilde{\sigma}(1 - \eta)(1 - \eta\beta)}{(1 + \eta + \beta\eta^2)} \left( \hat{i}_t - \pi_{t+1|t} \right) + \frac{1 - \eta}{1 + \eta(1 + \beta\eta)} \left[ \bar{c}_t - (\eta\beta + 1) \bar{c}_{t+1|t} + \eta\beta \bar{c}_{t+2|t} \right]
 \end{aligned} \tag{10}$$

172 where  $\bar{c}_t \equiv \log \bar{C}_t$  which, relaxing the habit persistence assumption, i.e.  $\eta = 0$ , boils  
 173 down to the basic New Keynesian IS curve. Next, loglinearizing the f.o.c. for the  
 174 firm's problem (9) with respect to sector  $m$  and  $s$ , we obtain

$$\pi_t^h = \kappa^h \left[ \omega + \varphi(1 + \eta^2\beta) \right] y_t - \kappa^h \varphi \eta y_{t-1} - \kappa^h \varphi \eta \beta y_{t+1|t} + \kappa^h \zeta_h (\rho\omega + 1) q_t \tag{11}$$

$$- \kappa^h \left[ (1 + \omega) a_t + \varphi(1 - \eta) (\bar{c}_t - \eta\beta \bar{c}_{t+1|t}) - \psi_t \right] + \beta \pi_{t+1|t}^h, \quad h = s, m,$$

175 where  $\omega \equiv \phi(v + 1) - 1$ ,  $\varphi \equiv \frac{1}{(1 - \eta)\tilde{\sigma}(1 - \eta\beta)}$ ,  $q_t \equiv \log \frac{Q_t}{Q}$ ,  $a_t \equiv \log A_t$ ,  $\psi_t^h \equiv \log \Psi_t$ , and

$$\kappa^h \equiv \frac{(1 - \alpha^h)(1 - \alpha^h\beta)}{\alpha^h(1 + \omega_h\theta)}, \tag{12}$$

$$\zeta_h \equiv \begin{cases} n_s > 0, & \text{if } h = m \\ -(1 - n_s) < 0, & \text{if } h = s \end{cases}. \quad (13)$$

It is worth noting that introducing heterogeneity in sectoral price stickiness the new variable  $q_t$  and the new relation between  $q_t$ ,  $\pi_t^s$ , and  $\pi_t^m$  enter in the model. The latter is captured by both (11) and the law of motion for  $q_t$  given by

$$q_t = q_{t-1} + \pi_t^s - \pi_t^m. \quad (14)$$

At this point two remarks are in order. First, considering (12), the shock elasticity of sectoral inflation in (11) is decreasing in the degree of sectoral price stickiness. This implies a shock filtering device for real shocks which is increasing with stickiness as described in Ascari, Flamini and Rossi (2012). Thus, the shock elasticity in the sector whose prices are stickier is smaller. Second, accounting for  $\zeta_h$ , the elasticities of sectoral inflations to the relative price  $q_t$  have opposite sign, and the sector whose prices are more flexible experiences (in absolute value) the larger elasticity. As it will be explained below, different sectoral shock elasticities and relative price elasticities activate a switching demand mechanism that buffers the impact of the symmetric shock on aggregate inflation.

Turning to the exogenous shocks, they are described by

$$\begin{aligned} a_{t+1} &= \gamma_a a_t + \varepsilon_{t+1}^a, \\ \bar{c}_{t+1} &= \gamma_c \bar{c}_t + \varepsilon_{t+1}^c, \\ \psi_{t+1} &= \gamma_\psi \psi_t + \varepsilon_{t+1}^\psi, \end{aligned}$$

where  $E_t(\varepsilon_{t+1}^h) = 0$ ,  $h = a, c, \psi$ . Log-linearizing the price index (4) we obtain aggregate inflation

$$\pi_t = n_s \pi_t^s + n_m \pi_t^m, \quad (15)$$

and substituting the sectoral inflations we obtain aggregate inflation in terms of lagged, current, and expected output gap, the relative price, expected inflation, and the exogenous shocks

$$\begin{aligned} \pi_t &= [\omega + \varphi(1 + \eta^2 \beta)] (n_s \kappa^s + n_m \kappa^m) y_t - \varphi \eta (n_s \kappa^s + n_m \kappa^m) y_{t-1} + \beta \pi_{t+1|t} \\ &\quad - \varphi \eta \beta (n_s \kappa^s + n_m \kappa^m) y_{t+1|t} - n_s n_m (\kappa^s - \kappa^m) (\rho \omega + 1) q_t \\ &\quad - (n_s \kappa^s + n_m \kappa^m) [(1 + \omega) a_t - \psi_t] - \varphi (1 - \eta) (n_s \kappa^s + n_m \kappa^m) (\bar{c}_t - \eta \beta \bar{c}_{t+1|t}). \end{aligned} \quad (16)$$

195 This aggregate New-Keynesian Phillips curve based on sectoral inflations boils down  
 196 to the standard New-Kenesian Phillips curve with habit persistence when sectoral  
 197 symmetry is imposed<sup>2</sup>, i.e.  $\alpha^s = \alpha^m$ . Finally, the model is closed with a Taylor rule  
 198 describing the behaviour of the central bank

$$i_t = \delta_0 i_{t-1} + (1 - \delta_0) \delta_1 \pi_t + (1 - \delta_0) \delta_2 y_t. \quad (17)$$

## 199 2.2 Calibration

200 Table 1a reports the calibration for the structural parameters based on the previous  
 201 literature. The degree of habits persistence  $\eta$  is set to 0.7; the elasticity of intertem-  
 202 poral substitution in consumption is  $\tilde{\sigma} = 2/3$ ; the intertemporal discount factor is  
 203  $\beta = 0.9975$  (3% per year); the coefficients of the Taylor rule are  $\delta_0 = 0.8$ ;  $\delta_1 = 1.5$ ;  
 204  $\delta_2 = 0.5/4$ . These values configure a quite standard calibration consistent, for exam-  
 205 ple, with Smets and Wouters (2007). Let us now turn to the remaining parameters.  
 206 The inverse of the elasticity of goods production (the inverse of Frish elasticity)  $\nu$  is set  
 207 to 1.17 as estimated by Fernández-Villaverde, Guerrón-Quintana and Rubio-Ramírez  
 208 (2010)<sup>3</sup>. Following Rotemberg and Woodford (1997), the elasticity of sectoral output  
 209 with respect to hours worked,  $1/\phi$ , is set to 0.75 and the sectoral elasticity of substi-  
 210 tution between any two differentiated goods  $\theta$  is set to 7.88 (average markup < 15%).  
 211 The elasticity of substitution between  $C_t^s$  and  $C_t^m$  in the CES consumption aggregate,  
 212  $\rho$ , is difficult to calibrate without specifying the type of industry the sectors belong  
 213 to. We then assume that the  $m$  and the  $s$  sector refer to the manufacturing and ser-  
 214 vices sectors respectively, and set  $\rho$  to 1 (Cobb-Douglas aggregator). Since this work  
 215 aims to insulate the impact of the asymmetry in sectoral price stickiness on economic  
 216 dynamics in presence of real shocks, sectors size is set to be equal, i.e. the number of  
 217 firms in the s-sector is  $n_s = 0.5$ ; and in the m-sector is  $n_m = 1 - n_s$ . Finally, the AR  
 218 coefficients of the exogenous processes are  $\gamma_a = \gamma_\psi = \gamma_c = 0.95$ , for any shock the  
 219 variance is  $\sigma_\varepsilon^2 = 0.009^2$ , and the sectoral degree of price stickiness  $\alpha_h$ ,  $h = s, m$  is let  
 220 free to vary in the range  $\{0.5, 0.6, 0.7, 0.8, 0.9\}$  as described in the analysis below.

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<sup>2</sup>Assuming also no habit persistence, i.e.  $\eta = 0$ , we obtain the basic New-Keynesian Phillips curve.

<sup>3</sup>This source for  $\nu$  is motivated by the fact that these authors use a set of priors nearly identical to the one proposed by Smets and Wouters (2007) in a similar DSGE model but specify the relation between the utility and labor in the same way of the current paper, which differs from Smets and Wouters (2007).

**Robustness** To check for the robustness of the results, we experimented an alternative calibration which is as close as possible to the one in Carvalho (2006)<sup>4</sup>. Table 1*b* only reports the parameters value of this second calibration which differ from the first calibration. Here there are no habits in consumption, i.e.  $\eta = 0$ , the elasticity of intertemporal substitution in consumption is  $\tilde{\sigma} = 1$ , the elasticity of sectoral output with respect to hours worked is  $1/\phi = 1$  (linear technology), and the inverse of the elasticity of goods production is  $\nu = 1$ . Finally, the sectoral elasticity of substitution between any two differentiated goods  $\theta$  and the elasticity of substitution between  $C_t^s$  and  $C_t^m$  in the CES consumption aggregate  $\rho$  are both set equal to 8.

### 3 Sectoral heterogeneity in price stickiness and economic dynamics

We now focus on the relation between sectoral heterogeneity in price stickiness and the dynamics of the economy in presence of positive cost-push, technology and household preferences shocks. All the shocks are supposed to hit symmetrically both sectors of the economy. The analysis first shows qualitatively via impulse response functions how dispersion in sectoral price stickiness affects the economic dynamics. Next, it assesses the policy mistakes for a central bank that ignores the presence of dispersion in sectoral price stickiness. Then the mechanics is explained focusing on the impact of the asymmetry assumption on the sectoral and aggregate AS. The mechanism at work is also illustrated using an appropriate AD-AS diagram for the New-Keynesian model. Finally, the investigation is completed looking at autocorrelations, and standard deviations of the endogenous variables.

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<sup>4</sup>Carvalho (2006) considers two alternative calibrations for  $\nu$  and  $\theta$ : either  $1/\nu = 0.5$  and  $\theta = 11$  or  $1/\nu = 1.5$  and  $\theta = 5$ . Here, for sake of simplicity but without loss in generality, we take the average values over these two calibrations, that is  $1/\nu = 1$  and  $\theta = 8$ . It is worth noting that in Carvalho (2006)  $\rho$  is set equal to the sectoral elasticity of substitution  $\theta$ , and it is reported that alternative calibrations for  $\rho$  including the case in which the CES is a Cobb-Douglas do not change the substantive findings.

### 3.1 Impulse responses to real shocks

Figures 1 shows the impulse response functions to a preference shock (Panel a), and to symmetric cost-push (Panel b) and technology shocks (Panel c) in presence of sectoral symmetry and asymmetry in the degree of price stickiness.

[INSERT FIGURE 1 HERE]

The first row of each Panel considers a two-sector economy under the *symmetry* assumption, i.e. price stickiness is the same in both sectors. Here the probability that a firm does not have the opportunity to optimize its price in a given period captured by  $\alpha_s$  and  $\alpha_m$  is set to 0.7. This value implies that, on average, firms revise their prices a bit less than every 3.5 quarters, which is consistent with Fernández-Villaverde, Guerrón-Quintana and Rubio-Ramírez (2010) and seems a natural benchmark of longer and shorter pricing cycle for firms belonging to different sectors. The second row, instead, considers the same economy under the *asymmetry* assumption but with the same mean of the symmetric economy. Specifically, the sectoral price stickiness are  $\alpha_s = 0.9$ ,  $\alpha_m = 0.5$ , resulting in the mean of 0.7 over the two sectors<sup>5</sup>. What is interesting here is that each panel reveals a common behaviour of aggregate inflation in response to an increasing degree of price stickiness asymmetry. This behaviour can be described as follows:

**Variance of sectoral price stickiness and aggregate inflation.** *For any shock considered, for a given mean value of price stickiness, the larger the variance (i.e. the larger the asymmetry), the lower the deviation of inflation from its steady state value, the lower the initial impact of the shock and the lower the persistence of the response to the shock<sup>6</sup>.*

Before explaining the mechanism that generates this result, we describe its implications on the behaviour of the interest rate and then on the economic dynamics. Starting with the preference shock, Panel a, it is worth noticing that this shock im-

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<sup>5</sup>The measure of price stickiness captured by  $\alpha$  in the Calvo's (1987) scheme varies a lot in the empirical literature ranging from 0.35 in Christiano et al. (2005) to 0.91 in Smets and Wouters (2003).

<sup>6</sup>Further analysis available upon request shows that this result is independent on the mean and the variance of sectoral price stickiness.

pacts on both the demand and supply side of the economy<sup>7</sup>, and these impacts go  
in opposite directions<sup>8</sup>. Plots for  $y$  and  $\pi$  then illustrate these effects, positive on  
the output gap and negative on inflation. Thus, two contrasting forces act on the  
interest rate via the Taylor rule. Now, under symmetry, first row, it occurs that the  
fall in inflation affects the interest rate more than the increase in the output gap  
leading the interest rate to fall in the initial periods. Yet, breaking the symmetry,  
second row, inflation is less affected by the shock and, therefore the negative impact  
on the interest rate is attenuated. This leaves the interest rate more exposed to the  
positive impact of the output gap. Consequently, the monetary policy turns out to  
be more active in the subsequent periods in order to focus on the stabilization of the  
output gap. Hence, given the relation between the variance of sectoral price stickiness  
and aggregate inflation, monetary policy can better stabilize the output gap under  
asymmetry.

Moving to a cost-push or technology shock, the economy turns out to be hit only  
through the supply side. Thus the larger the asymmetry, the less the shock affects  
aggregate inflation. This implies that the interest rate has to respond less via the  
Taylor rule and thus that the shock propagates less to the output gap. Accordingly,  
Panels b and c show that the policy response in the asymmetric economy tends  
to be remarkably milder than in the symmetric one. Similarly, the deviations of  
output-gap and inflation from their steady state values in the asymmetric economy  
tend to be remarkably smaller than in the symmetric economy. Summing up, with  
supply shocks, heterogeneity in sectoral price stickiness tends to buffer exogenous  
disturbances requiring a less active monetary policy.

### 3.2 Monetary policy mistakes ignoring sectoral price stickiness heterogeneity

The previous findings imply that two two-sector economies sharing the same mean  
degree of price stickiness but not the same variance respond differently to exogenous  
real disturbances and therefore require specific monetary policies. This implication

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<sup>7</sup>The preference shock is a shock to the utility function so that it affects, on the one hand, the Euler equation and therefore the aggregate demand and, on the other hand, the marginal rate of substitution between labour and consumption entering in the optimal supply of labour, and therefore the aggregate supply.

<sup>8</sup>Indeed in equation (10) the coefficient of the preference shock is positive and in equation (16) it is negative.

297 poses serious problems in terms of monetary policy mistakes for central banks that  
 298 neglects sector price stickiness heterogeneity. To illustrate this point, we can consider,  
 299 for instance, a two-sector economy where  $\alpha_s = 0.9$  and  $\alpha_m = 0.5$  so that the average  
 300 degree of price stickiness is  $\alpha = 0.7$ . In this economy, we let the central bank assume  
 301 that  $\alpha_s = \alpha_m = 0.7$ , or, equivalently for what is shown below, only consider the aver-  
 302 age price stickiness value disregarding the dispersion across sectors. Then, exogenous  
 303 shocks hit and the central bank responds. Yet, the actual response will be different  
 304 from the response that would occur if the central bank considered heterogeneity in  
 305 sectoral price stickiness, i.e. the correct response. To develop this argument, let us  
 306 define as *monetary policy* the current and expected interest rate decisions, that is  
 307 the interest rate path following the shock<sup>9</sup>. There are, then, two monetary policies:  
 308 the actual and the correct one, and we can ask what the policy mistakes are for the  
 309 central bank that neglects the dispersion in sectoral price stickiness.

310 Figure 2 provides a *prima facie* answer contrasting in each panel the IRFs of the  
 311 interest rate capturing the actual (dashed) and the correct policy (solid). Here each  
 312 panel lies on a row referring to a calibration and on a column referring to a shock.

313 [INSERT FIGURE 2 HERE]

314 Figure 2 shows that asymmetry in price stickiness always makes monetary policy  
 315 remarkably different. With a cost-push shock,  $\varepsilon^\psi$ , the actual policy is uniformly  
 316 *tighter* than the correct one, while with a technology shock,  $\varepsilon^a$ , the actual is uniformly  
 317 *easier* than the correct; these results holding with both calibrations. Left with a  
 318 preference shock,  $\varepsilon^c$ , under the first calibration the actual policy is *less tight* than  
 319 the correct one, except for the initial three periods. Under the second calibration  
 320 the actual policy is fully wrong: it is *easy* instead of *tight* as required by the correct  
 321 policy.

322 Visual inspection thus reveals that neglecting asymmetry in price stickiness leads  
 323 to quantitative and qualitative policy mistakes. At this point, to sharp our evaluation  
 324 of these policy mistakes we need to measure the policy error. For this purpose, let us  
 325 introduce a policy error statistic in two steps: first computing the distance between  
 326 the interest rate path under symmetry and asymmetry at each point in time. Then  
 327 dividing this distance by the value of the policy under asymmetry at each point in

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<sup>9</sup>This definition is introduced to avoid confusion between the *monetary policy rule*, which here is the Taylor rule and is invariant to the symmetry/asymmetry case, and the *monetary policy*, that is the decisions (current and expected) taken by the central bank using the policy rule.

time. What results is therefore the *percentage deviation of the actual policy from the correct policy*. Figure 3 reports this statistic for the policy errors. As before, each panel lies on a row that refers to a calibration and to a column that refers to a shock.

[INSERT FIGURE 3 HERE]

In addition, now, each panel shows for every point in time the measure (in percentage terms) and the type of the error (e.g. policy tighter, easier, etc.). To fix the ideas, we can consider the policy errors with a cost-push shock under the first calibration (row1, column 1). Looking at the tenth period subsequent to the shock, the actual policy turns out to be 100% tighter than the correct one. Now, what Figure 3 reveals is that the policy errors are generally very large, with actual policies that compared to the correct ones can be easier (black), tighter (blue/dark grey), less tight (white) between 40% and 145% over the first ten periods. Or with policies that are easy instead of tight (yellow/light grey), with a distance between the two which is no less than 150% of the (absolute) value of the correct tight policy. Summing up, Table 2 reports that the percentage deviation of the actual policy from the correct policy averaged over the first ten periods is between 50% and 100% for the cost-push and technology shock, and between 60% and 180% for the preference shock.

Now, before deepening the investigation with a quantitative assessment of the implications of this policy mistakes, it is worth stopping for a natural question: what drives these findings?

### 3.3 Mechanics

When sectors differ in terms of stickiness, sectoral inflations differ after a shock and the stickier sector experiences a smaller change in inflation<sup>10</sup>. As a result the relative price between sectors kicks in as shown by equation (14) and tends to divert the demand from the sector whose goods are relatively more expensive to the sector whose goods are relatively cheaper. As expected, in the former sector inflation falls while in the latter increases. Yet, these sectoral inflation changes caused by  $q$ , beyond differing in direction, differ also size wise because the change in marginal costs caused by the demand change impacts less inflation in the stickier sector. This is due to the fact that the elasticity of sectoral inflation to the relative price is decreasing in sectoral

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<sup>10</sup>This holds no matter what the shock is: with a supply shock through the shock filtering mechanism and with a demand shock through a different slope of the Phillips curve.

358 stickiness as shown in (11) and therefore is smaller in the stickier sector. Such a  
 359 difference in the impact of the relative price on sectoral inflations implies a fall in  
 360 aggregate inflation and therefore a buffering role played by the switching demand  
 361 mechanism. It is worth noting that the sector where prices are more flexible, while  
 362 exposing aggregate inflation more to the shocks, is also the one through which the  
 363 switching demand mechanism acts the most to buffer the shock.

364 The buffering device activated by heterogeneity in price stickiness can be conve-  
 365 niently illustrated with a New Keynesian AS-AD framework that gives special atten-  
 366 tion to the role played by expectations.

### 367 **3.3.1 A New Keynesian AS-AD graphical illustration of the role of price** 368 **stickiness dispersion**

369 The AD-AS diagram is presented in the  $(\pi_t, y_t)$  space. For sake of simplicity but with-  
 370 out loss in generality the assumptions of habit persistence and interest rate smoothing  
 371 are relaxed, i.e.  $\eta = 0$  and  $\delta_0 = 0$ . Drawing the diagram, it is worth recalling that in  
 372 steady state all the expectations terms are zero.

373 To obtain the AD we join the Euler equation and the Taylor rule and solve for  
 374 current inflation as a function of the current output gap given the output gap and  
 375 inflation expectations

$$\pi_t = - \left( \frac{1 + \tilde{\sigma}\delta_2}{\tilde{\sigma}\delta_1} \right) y_t + \frac{1}{\tilde{\sigma}\delta_1} y_{t+1|t} + \frac{1}{\delta_1} \pi_{t+1|t}. \quad (18)$$

376 Solving this equation forward leads to

$$\pi_t = - \left( \frac{1 + \tilde{\sigma}\delta_2}{\tilde{\sigma}\delta_1} \right) y_t + \frac{\delta_1 - 1 - \tilde{\sigma}\delta_2}{\tilde{\sigma}\delta_1} \sum_{\tau=1}^{\infty} \delta_1^{-\tau} y_{t+\tau|t}. \quad (19)$$

377 Equation (19) shows that the relation between current inflation and output gap  
 378 shifts in the  $(\pi_t, y_t)$  space according to the expected path of the output gap. Thus,  
 379 if breaking the symmetry changes this expected path there will be a shift of the AD  
 380 with respect to its position under symmetry.

Regarding the AS, equation (16) can be solved forward to obtain

$$\begin{aligned} \pi_t = & (\omega + \varphi) \frac{1}{2} (\kappa_s + \kappa_m) y_t + \frac{1}{2} (\omega + \varphi) (\kappa_s + \kappa_m) \sum_{\tau=1}^{\infty} \beta^\tau y_{t+\tau|t} \\ & - \frac{1}{4} (\rho\omega + 1) (\kappa_s - \kappa_m) \sum_{\tau=0}^{\infty} \beta^\tau q_{t+\tau|t} + \frac{1}{2} (\kappa_s + \kappa_m) \sum_{\tau=0}^{\infty} \beta^\tau \psi_{t+\tau|t}, \end{aligned} \quad (20)$$

which under symmetry boils down to

$$\pi_t = (\omega + \varphi) \frac{1}{2} \kappa y_t + \frac{1}{2} (\omega + \varphi) \kappa \sum_{\tau=1}^{\infty} \beta^\tau y_{t+\tau|t} + \frac{1}{2} \kappa \sum_{\tau=0}^{\infty} \beta^\tau \psi_{t+\tau|t}, \quad (21)$$

where  $\kappa = \kappa_s = \kappa_m$ . For a given expected path of the cost-push shock, equation (20) shows that current inflation depends on the expected paths of the output gap and the relative price, while equation (21) shows that it depends only on the expected path of the output gap.

### 3.3.2 Cost-push shock case

Figure 4 reports the *steady state equilibrium A* and the *off-steady state equilibria* in presence of a cost-push shock under symmetry *B* ( $\alpha_m = \alpha_s = 0.7$ ), and asymmetry *C* ( $\alpha_m = 0.6$ ,  $\alpha_s = 0.8$ ) and *D* ( $\alpha_m = 0.5$ ,  $\alpha_s = 0.9$ ).

[INSERT FIGURE 4 HERE]

Off the steady state, Figure 4 takes a snapshot of  $\pi_t$  and  $y_t$  in the initial period in which the shock hits the economy. It does not leaves aside the subsequent periods though. Indeed, expectations on the economic dynamics determine the position of the AD and AS (not their slopes) as shown by equations (19-21). Describing the Figure, the red/grey and the black color refer to symmetry and asymmetry respectively, while the solid lines refer to the steady state equilibrium, and the dash and dots lines refer to off-steady state equilibria. It is worth noting that in steady state the AD (downward sloped) under symmetry and asymmetry coincide, while the AS (upward sloped) is steeper under asymmetry<sup>11</sup>.

Figure 4 shows that under symmetry, when the shock hits the economy the equilibrium is no longer A but B. What happens is that with the shock the expected path for inflation becomes positive so that, via the Taylor rule, the expected path for the output gap becomes negative. As shown by equations (21 and 19), this leads the AD to shift left and the AS to shift up (the impact of the shock prevails on the deflationary path for the output gap). Breaking the symmetry the economy moves either to *C* (low asymmetry) or to *D* (high asymmetry). With respect to equilibrium

<sup>11</sup>Breaking the symmetry, the elasticity of inflation to the output gap and the shock increases. This effect, visible in the AS steeper under asymmetry and due to the convexity of the relation between  $\kappa$  and  $\alpha$ , exerts a minor impact on the macroeconomic dynamics.

407 B, equilibria  $C$  and  $D$  feature a smaller increase in inflation and a smaller fall in out-  
 408 put. Furthermore, the larger the asymmetry, the larger the departure from  $B$  and the  
 409 larger these effects. Indeed, regarding the AS, for a given current value and expected  
 410 path of the shock, under asymmetry the shift is determined by the expected path of  
 411 the output gap and the relative price, summarized in (20) by the terms  $\sum_{\tau=1}^{\infty} \beta^{\tau} y_{t+\tau|t}$   
 412 and  $\sum_{\tau=0}^{\infty} \beta^{\tau} q_{t+\tau|t}$  respectively. In contrast, given the shock, under symmetry the shift is  
 413 determined only by the expected path of the output gap. Thus, in buffering the shock  
 414 the *deflating mechanism* provided by the output gap is supported by the *switching*  
 415 *demand mechanism* provided by the relative price. This is shown by the *negative*  
 416 expected path for  $q$  reported in Panel b of Figure 1 associated with the positive elas-  
 417 ticity of aggregate inflation to the relative price in equation (20). Thus the expected  
 418 path of the relative price buffers the shock in addition to the expected path for the  
 419 output gap in (20). As a result of the presence of the switching demand mechanism,  
 420 the AS shifts up less under asymmetry.

421 Regarding the AD, the smaller shift to the left under asymmetry is always due to  
 422 the presence of the relative price. Indeed, the smaller impact of the shock on inflation  
 423 due to the switching demand mechanism implies, via the policy response, a smaller  
 424 deflating role imposed to the output gap, which is captured by a smaller value of  
 425 the term  $\sum_{\tau=1}^{\infty} \beta^{\tau} y_{t+\tau|t}$  in (19). Summing up, breaking the symmetry results in different  
 426 impacts of the cost-push shock on sectoral inflations which, activating the relative  
 427 price, allows a partial return of both AS and AD to their pre-shock positions. Hence  
 428 breaking the symmetry results in lower output and inflation volatility.

### 429 **3.4 Persistence and volatility of the macrovariables vs sec-** 430 **toral price stickiness heterogeneity**

431 The Impulse Response analysis has signalled two consequences of the presence of  
 432 sectoral price stickiness asymmetry in the working of the economy. On the one  
 433 hand it affects the macroeconomic dynamics. On the other hand, if it is neglected in  
 434 monetary policy decisions, it leads to quantitative and qualitative policy mistakes. In  
 435 order to further characterize these consequences, it is useful to focus on the *persistence*  
 436 and *volatility* of  $y$ ,  $i$ , and  $\pi$  and studying how they change as a function of sectoral  
 437 price stickiness asymmetry.

Starting with persistence, this feature of the dynamics is here measured using, for each variable, the sum of the first five autocorrelation coefficients<sup>12</sup>. Figure 5, Panel a, shows that the persistence of  $y$ ,  $i$ , and in particular  $\pi$ , monotonically decreases for increasing degrees of sectoral price stickiness asymmetry.

[INSERT FIGURE 5 HERE]

Specifically, moving from  $\alpha_m = \alpha_s = 0.7$  to  $\alpha_m = 0.5$ ,  $\alpha_s = 0.9$ , the persistence of  $y$ ,  $i$  and  $\pi$  decreases of 2.6%, 6.9%, and 24% respectively. Noting that in the two sectors inflation persistence exhibits opposite behaviors, the stark fall in aggregate inflation persistence depends on the major role played by the sector where prices are more flexible, i.e. the m-sector. Indeed, the larger the asymmetry, the more the m-sector is exposed to the destabilizing impact of the shock and to the stabilizing impact of the switching demand mechanism; both factors contracting persistence. In contrast, the larger the asymmetry, the less the s-sector is exposed to the destabilizing impact of the shock and to the stabilizing impact of the switching demand mechanism<sup>13</sup>. The decrease in inflation persistence leads, in turn, to a decrease in the interest rate persistence via the Taylor rule.

The finding that heterogeneity in price stickiness leads to less inflation persistence questions the ability of the standard New Keynesian Phillips curve in fitting the macroeconomic evidence on inflation persistence, a view that this work shares with Sheedy's (2007).

Let us now turn to the volatility of  $y$ ,  $i$ , and  $\pi$  as a function of the asymmetry in sectoral price stickiness. The impulse response analysis signalled that introducing sectoral asymmetry in price stickiness tends to reduce the deviations of these variables from their long run values. Consistently, Figure 5, Panel b shows that the unconditional standard deviations of these variables monotonically fall when the asymmetry in sectoral price stickiness increases<sup>14</sup>. In particular, the variability of  $\pi$  and  $i$  decreases of 38.2% leading to a decrease of the variability of  $y$  of the 31.3%. This finding matters as indicates that sectoral asymmetry in price stickiness plays a key role in determining the variability of the endogenous variables.

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<sup>12</sup>The autocorrelation coefficients have been computed in presence of the whole set of considered shocks.

<sup>13</sup>This depends on the elasticities of sectoral inflations to real shocks and the relative price as explained above.

<sup>14</sup>In the Figure, the inflation and the interest rate volatility curve tend to overlap so that the inflation curve is hidden.

467 These results also imply that two economies that share the average but not the  
468 variance of the sectoral price stickiness exhibit very different persistence and variabil-  
469 ity of the endogenous variables.

470 At this point it is interesting to relate the current results to the inflation targeting  
471 operating procedure in use at several central bank (Svensson 2010). Sketching this  
472 procedure, first the staff computes alternative distribution forecasts associated with  
473 different interest rate paths minimizing a standard loss function. Then the Board  
474 selects the policy associated with the specific distribution forecast that suits best its  
475 preferences. The current results thus suggest that one-sector models are not suitable  
476 to obtain projections of the target variables since they can be highly misleading as  
477 to their persistence and volatility.

478 Finally, these theoretical results are in line with the empirical evidence related  
479 to French data found by Imbs et al. (2011). Indeed, they show that in presence of  
480 sectoral heterogeneity in price stickiness, sectoral estimates imply policies associated  
481 with volatilities in output gap and inflation that halve the ones implied by aggregate  
482 data.

## 483 **4 Shocks and policy pitfalls of one-sector model** 484 **with price stickiness heterogeneity**

485 The role played by price stickiness heterogeneity in the transmission of monetary  
486 shocks has been pioneered by Carvalho (2006). Therein the important result has been  
487 to show that the presence of sectoral differences results in *larger* and *more persistent*  
488 effects of monetary shocks on the output gap. Comparing the current findings with  
489 Carvalho's we observe that they tend to be opposite: with real shocks the presence of  
490 sectoral differences in prices stickiness results in *smaller* effects on the output gap<sup>15</sup>.

491 Two questions then naturally arise: why does this happen? and is there any gen-  
492 eral result holding for *any* exogenous shock that can be useful for policy analysis? To  
493 address the first question we simulate the response of the current model to a monetary  
494 shock and illustrate the result using the previous AD-AS graphical framework.

495 Adding a monetary shock to the Taylor rule specified as  $m_{t+1} = \gamma_m m_t + \varepsilon_{t+1}^m$  the  
496 forward solution of the AD given by (19) is replaced by

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<sup>15</sup>Previous analysis has shown that output gap persistence falls too, but to a minor extent.

$$\pi_t = - \left( \frac{1 + \tilde{\sigma}\delta_2}{\tilde{\sigma}\delta_1} \right) y_t + \frac{\delta_1 - 1 - \tilde{\sigma}\delta_2}{\tilde{\sigma}\delta_1} \sum_{\tau=1}^{\infty} \delta_1^{-\tau} y_{t+\tau|t} - \frac{1}{\delta_1} \sum_{\tau=0}^{\infty} \left( \frac{1}{\delta_1} \right)^{\tau} m_{t+\tau|t}. \quad (22)$$

Equation (22) shows that a monetary policy shock shifts the AD in the  $(\pi_t, y_t)$  space. Since the position of the AD depends also on the expected path of the output gap, if breaking the symmetry changes this path then there will be a different impact of the monetary shock. To illustrate the relevant role played by the asymmetry assumption, Figure 6 considers a contractionary monetary policy shock.

[INSERT FIGURE 6 HERE]

With both symmetry and asymmetry, the shock leads to a *negative* expected path for the output gap which, in turn, leads to a *negative* expected path for inflation. This leads the AD to shift left and the AS to shift down, point B. What happens when we break the symmetry? breaking the symmetry the AS shifts up and the AD shifts further left, point C (low asymmetry) or D (high asymmetry). Starting with the AS, the deflationary impact of the contractionary monetary policy will be smaller in the sector with stickier prices. Thus, the relative price  $q$  leaves the steady state and increases. This, in turn, exerts a positive effect on aggregate inflation contrasting the shift down of the AS determined by the negative expected output gap<sup>16</sup>.

Turning to the AD, why does it shift further left when we break the symmetry? Because, as explained above the switching demand mechanism prevents the expected inflation path from deviating from its steady state value as much as with symmetry. This implies that the policy response via the Taylor rule to inflation is smaller than under symmetry. As a result, the initial impact of the shock on the output gap is larger and the subsequent path to its steady state takes longer.

Let us now turn to the second question: is there any general result useful for policy analysis that we can apply to any exogenous shocks in presence of sectoral differences in price stickiness? Drawing on the AS-AD illustrations for the cost-push and monetary shock, Figures 4 and 6, we can note that, independently on the nature of the shock, breaking the symmetry contracts the outward shift of the AS. This contraction is due to the buffering device activated by the switching demand mecha-

<sup>16</sup>Since the elasticity of current inflation to  $q$  is positive due to the fact that with asymmetry  $\kappa_s < \kappa_m$ , the  $q$  effect on aggregate inflation is positive.

nism<sup>17</sup>. It is easy to show that this result is general in that applies to technology and preference shocks too. Thus, with any shock, sectoral differences in price stickiness lead to smaller and less persistent effects on inflation. This suggests three policy pitfalls for policy makers grounding policy decisions on one-sector model when the actual economy features sectoral differences in price stickiness. First, with *any* shock the one-sector model will *overvalue* the variation and persistence of inflation. Second, with real shocks the one-sector model will *overvalue* the variation of the output gap. Third, with monetary shocks the one-sector model will *undervalue* the variation and persistence of the output gap. Table 3 reports these policy pitfalls.

## 5 Concluding remarks

Using a two-sector New-keynesian model, this paper investigates how sectoral heterogeneity in price stickiness affects the dynamics of the economy in presence of real shocks.

When sectoral symmetry is broken, the relative price between sectoral goods appears into the working of economy and significantly alters its response to exogenous shocks via the demand channel. As a result, asymmetry in sectoral price stickiness on the one hand leads to an important fall in the persistence of aggregate inflation and to a moderate fall in the persistence of the interest rate. On the other hand, it leads to an important fall in the volatility of inflation, the interest rate and the output gap. Thus, two economies differing in the dispersion of sectoral asymmetry but not in the mean may exhibit very unlike volatility and persistence.

This finding has important monetary policy implications. Disregarding the dispersion in sectoral price stickiness leads policymakers first to overvalue the variation and persistence of inflation; second, to overvalue the variation of the output gap. We show that this wrong evaluation of the aggregate dynamics can lead policymakers to relevant mistakes in presence of real shocks. They can follow over the first ten quarters subsequent the shock a policy that is qualitatively different from the correct one, or a policy that is up to 150% tighter or easier than the correct one. These

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<sup>17</sup>Formally, in both cases the shock leads to an expected path for  $q$  whose sign is opposite to the sign of the elasticity of  $\pi_t$  with respect to the shock at issue. Indeed, with a cost-push shock that has a direct positive impact on  $\pi_t$  it happens that  $q$  exhibits a negative path. With a monetary shock that has an indirect negative impact on  $\pi_t$  (via the expected path for the output gap), it happens that  $q$  exhibits a positive path.

implications suggests that policy decisions should seriously account for the presence of sectoral price stickiness. Moreover, they highlight the relevance of sectoral data for economic estimations and forecasts.

Considering a country or monetary union where regions or states feature different degree of price stickiness, the current findings question the appropriateness of a monetary policy based on the average degree of price stickiness. Further analysis will investigate this point as well as how sectoral size and strategic complementarities affect the relation between sectoral asymmetry in price stickiness and the dynamics of the economy.

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TABLE 1 Alternative calibrations

Panel a -benchmark		Panel b -robustness			
$\eta$	0.7	$n_s$	0.5	$\eta$	0
$\tilde{\sigma}$	2/3	$n_m$	0.5	$\tilde{\sigma}$	1
$\beta$	0.9975	$\gamma_a$	0.95		
$\rho$	1	$\gamma_\psi$	0.95	$\rho$	8
$\nu$	1.17	$\gamma_c$	0.95	$\nu$	1
$1/\phi$	0.75	$\sigma_\varepsilon^2$	0.009 <sup>2</sup>	$1/\phi$	1
$\theta$	7.88			$\theta$	8
$\delta_0$	0.8				
$\delta_1$	1.5				
$\delta_2$	0.5/4				

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TABLE 2. Average Policy Error for the First Ten Periods

Calibration	Shock		
	$\varepsilon_\psi$	$\varepsilon_a$	$\varepsilon_c$
1	50%	50%	60%
2	100%	100%	180%

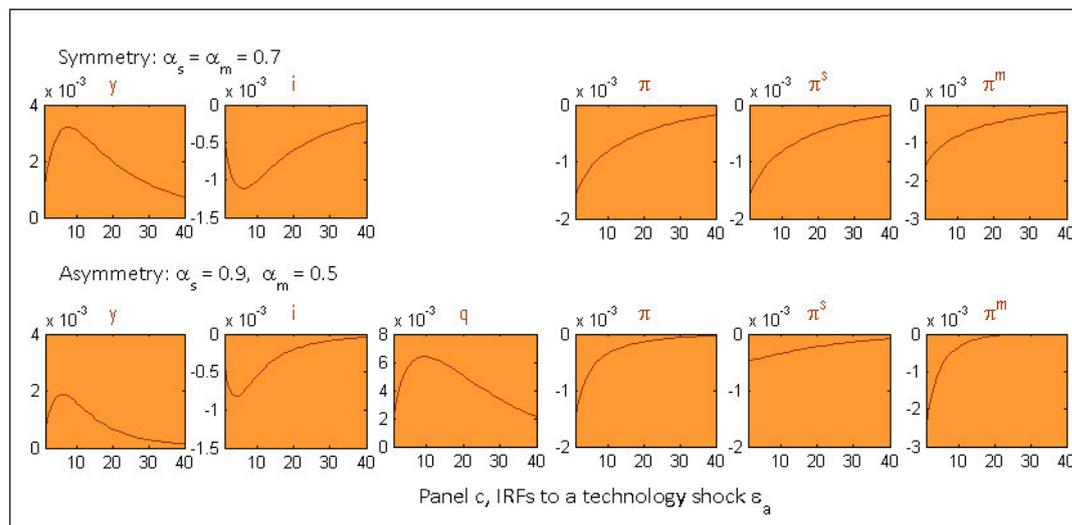
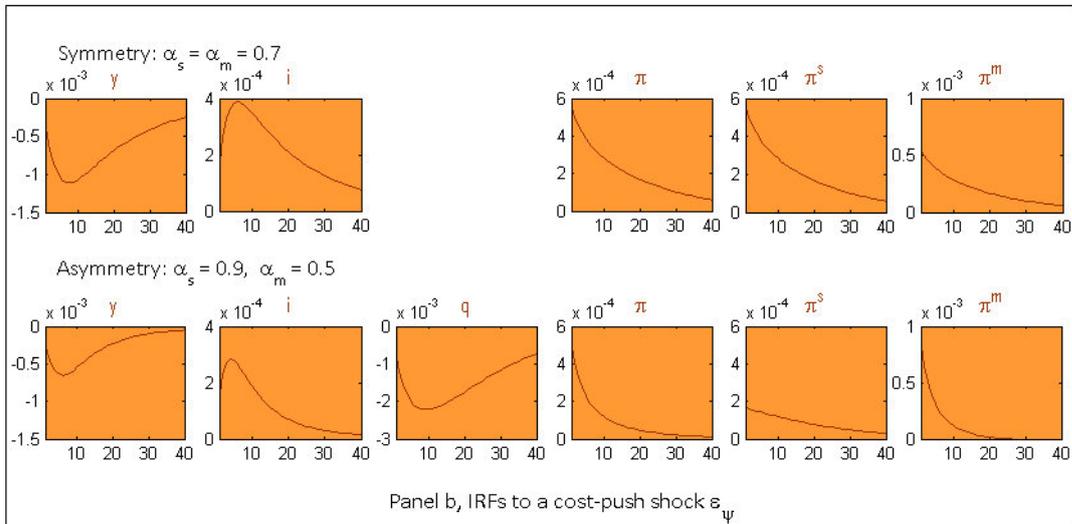
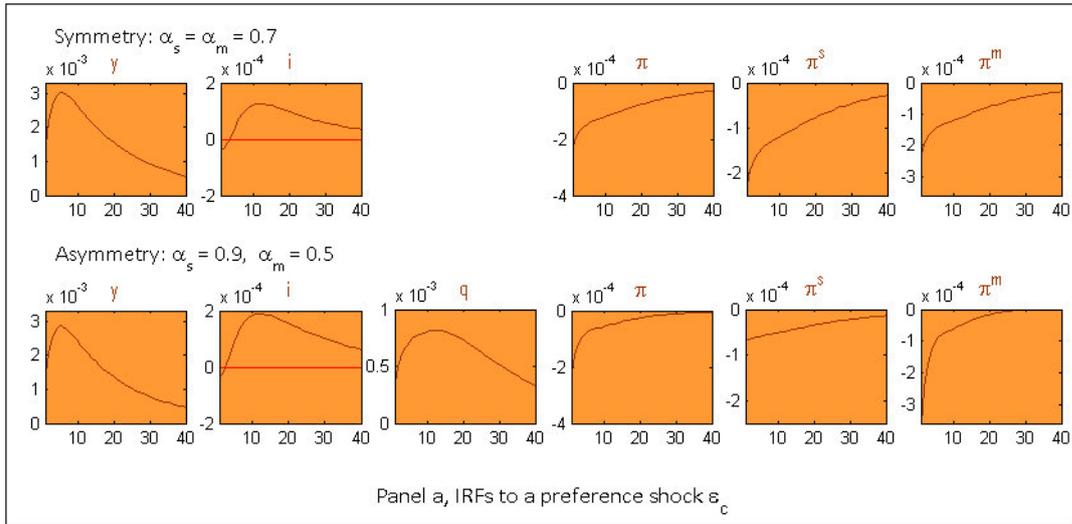
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TABLE 3. Policy pitfalls using one-sector models in presence of price stickiness asymmetry

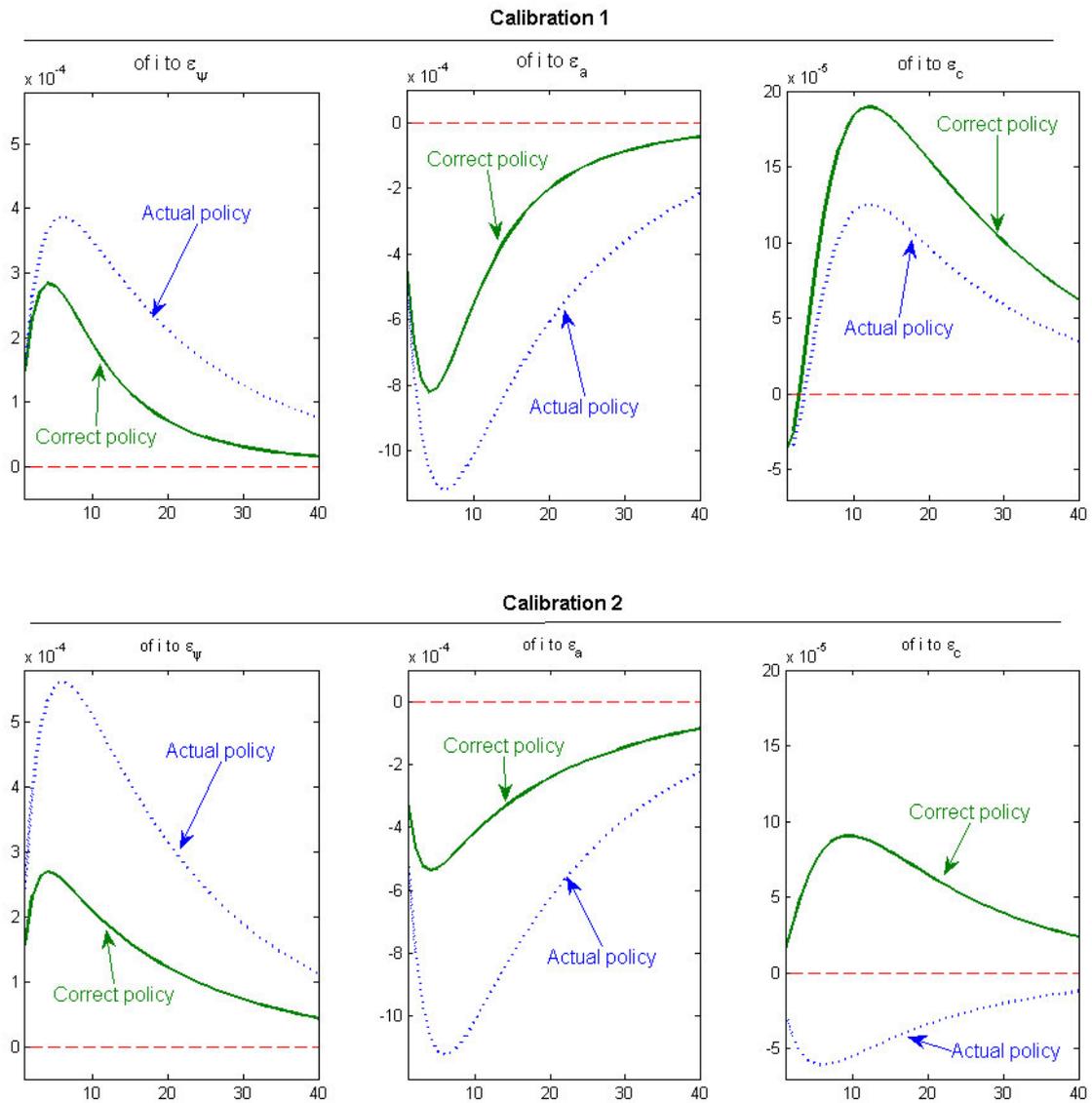
		Shock	
		Real	Monetary
$\pi$	Overvaluation of persistence and variation		Overvaluation of persistence and variation
$y$	Overvaluation of variation		Undervaluation of persistence and variation

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**Figure 1. IRFs to real shocks in presence of symmetry and asymmetry in sectoral price stickiness**



**Figure 2. IRFs of the interest rate to real shocks under sectoral price stickiness symmetry (actual policy) and asymmetry (correct policy)**



**Figure 3. Monetary policy mistakes in presence of real shocks: percentage deviation of the actual policy from the correct policy**

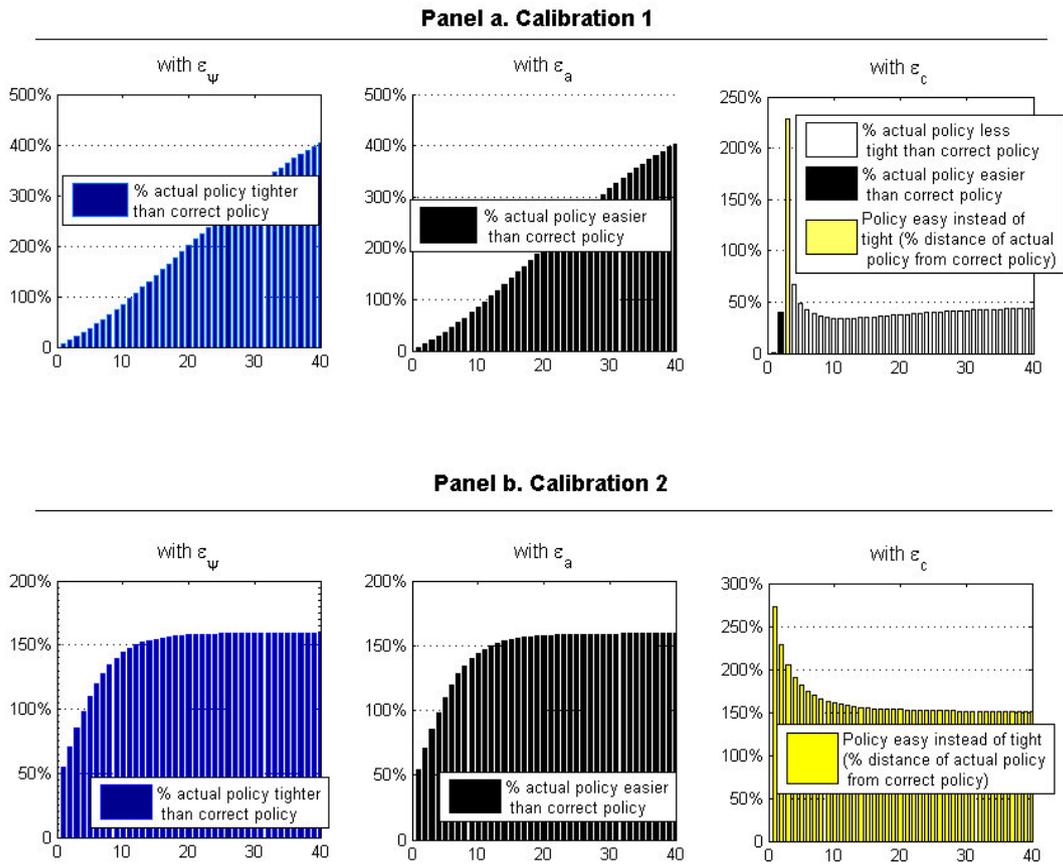
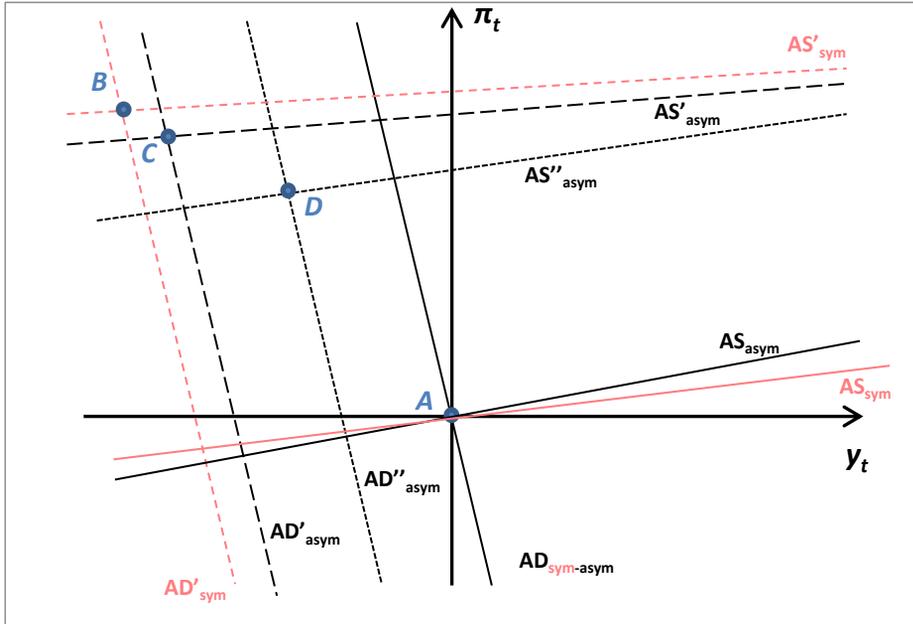
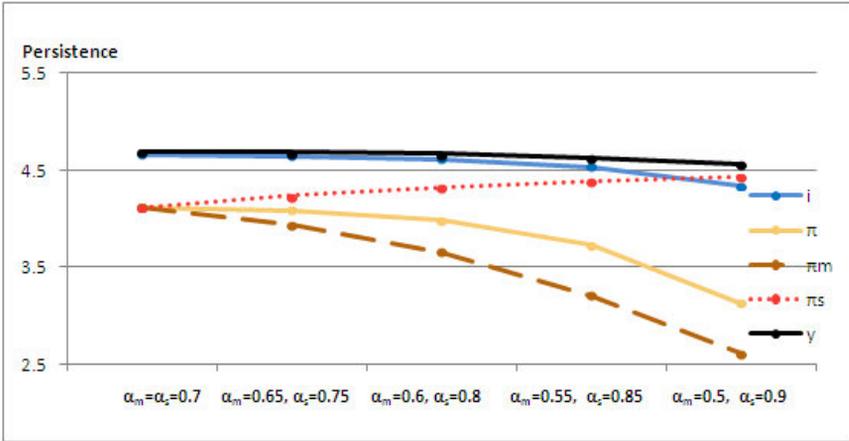


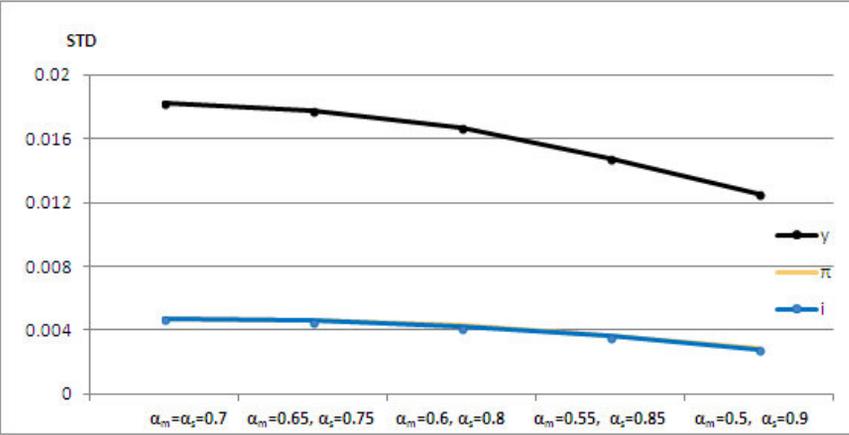
Figure 4. Steady state equilibrium and off-steady state equilibria after a cost-push shock with symmetry and asymmetry in sectoral price stickiness.



**Figure 5. Persistence and volatility of the macrovariables vs asymmetry in sectoral price stickiness**



**Panel a. Persistence vs asymmetry in sectoral price stickiness**



**Panel b. Volatility vs asymmetry in sectoral price stickiness**

Figure 6. Steady state equilibrium and off-steady state equilibria after a monetary shock with symmetry and asymmetry in sectoral price stickiness.

